

11.2

Special Right Triangles

For use with Exploration 11.2

Essential Question What is the relationship among the side lengths of 45°-45°-90° triangles? 30°-60°-90° triangles?

1 EXPLORATION: Side Ratios of an Isosceles Right Triangle

Go to *BigIdeasMath.com* for an interactive tool to investigate this exploration.

Work with a partner.

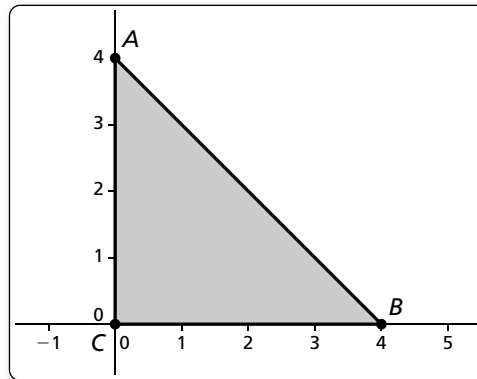
- a. Use dynamic geometry software to construct an isosceles right triangle with a leg length of 4 units.
- b. Find the acute angle measures. Explain why this triangle is called a 45°-45°-90° triangle.

- c. Find the exact ratios of the side lengths (using square roots).

$$\frac{AB}{AC} = \underline{\hspace{2cm}}$$

$$\frac{AB}{BC} = \underline{\hspace{2cm}}$$

$$\frac{AC}{BC} = \underline{\hspace{2cm}}$$



Sample

Points

$A(0, 4)$

$B(4, 0)$

$C(0, 0)$

Segments

$AB = 5.66$

$BC = 4$

$AC = 4$

Angles

$m\angle A = 45^\circ$

$m\angle B = 45^\circ$

- d. Repeat parts (a) and (c) for several other isosceles right triangles. Use your results to write a conjecture about the ratios of the side lengths of an isosceles right triangle.

11.2 Special Right Triangles (continued)

2 EXPLORATION: Side Ratios of a 30°-60°-90° Triangle

Go to *BigIdeasMath.com* for an interactive tool to investigate this exploration.

Work with a partner.

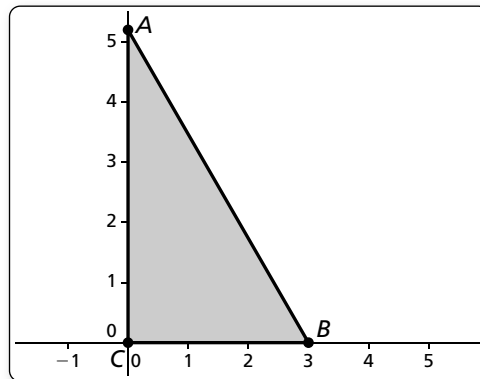
- a. Use dynamic geometry software to construct a right triangle with acute angle measures of 30° and 60° (a 30°-60°-90° triangle), where the shorter leg length is 3 units.

- b. Find the exact ratios of the side lengths (using square roots).

$$\frac{AB}{AC} = \underline{\hspace{2cm}}$$

$$\frac{AB}{BC} = \underline{\hspace{2cm}}$$

$$\frac{AC}{BC} = \underline{\hspace{2cm}}$$



Sample
Points
 A(0, 5.20)
 B(3, 0)
 C(0, 0)
Segments
 AB = 6
 BC = 3
 AC = 5.20
Angles
 m∠A = 30°
 m∠B = 60°

- c. Repeat parts (a) and (b) for several other 30°-60°-90° triangles. Use your results to write a conjecture about the ratios of the side lengths of a 30°-60°-90° triangle.

Communicate Your Answer

- 3. What is the relationship among the side lengths of 45°-45°-90° triangles? 30°-60°-90° triangles?

11.2

Practice

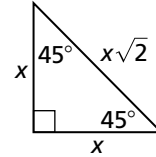
For use after Lesson 11.2

Theorems

45°-45°-90° Triangle Theorem

In a 45°-45°-90° triangle, the hypotenuse is $\sqrt{2}$ times as long as each leg.

Notes:

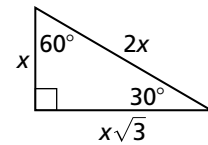


$$\text{hypotenuse} = \text{leg} \cdot \sqrt{2}$$

30°-60°-90° Triangle Theorem

In a 30°-60°-90° triangle, the hypotenuse is twice as long as the shorter leg, and the longer leg is $\sqrt{3}$ times as long as the shorter leg.

Notes:



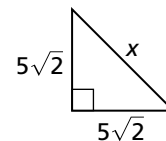
$$\begin{aligned} \text{hypotenuse} &= \text{shorter leg} \cdot 2 \\ \text{longer leg} &= \text{shorter leg} \cdot \sqrt{3} \end{aligned}$$

Worked-Out Examples

Example #1

Find the value of x . Write your answer in simplest form.

$$\begin{aligned} \text{hypotenuse} &= \text{leg} \cdot \sqrt{2} \\ x &= 5\sqrt{2} \cdot \sqrt{2} \\ x &= 5\sqrt{4} \\ x &= 5 \cdot 2 = 10 \end{aligned}$$

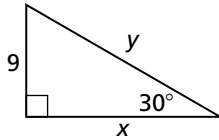


11.2 Practice (continued)

Example #2

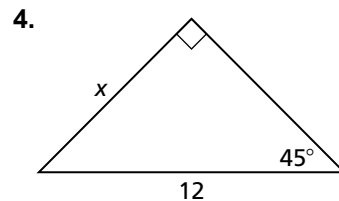
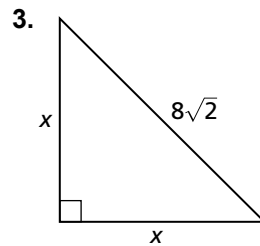
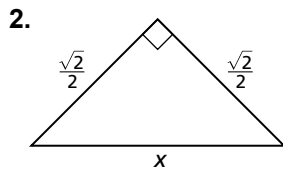
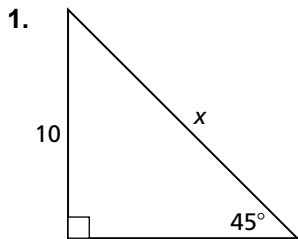
Find the values of x and y . Write your answers in simplest form.

longer leg = shorter leg $\cdot \sqrt{3}$
 $x = 9\sqrt{3}$
 hypotenuse = $2 \cdot$ shorter leg
 $y = 2 \cdot 9$
 $y = 18$

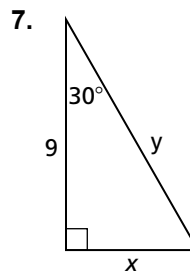
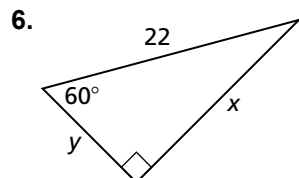
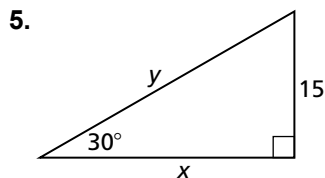


Practice A

In Exercises 1–4, find the value of x . Write your answer in simplest form.



In Exercises 5–7, find the values of x and y . Write your answers in simplest form.

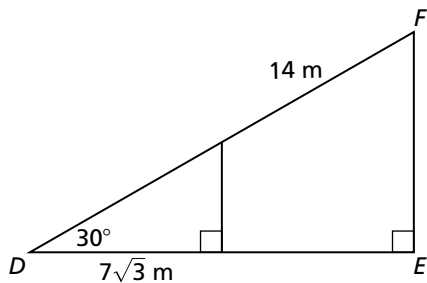


11.2 Practice (continued)

In Exercises 8 and 9, sketch the figure that is described. Find the indicated length.
Round decimal answers to the nearest tenth.

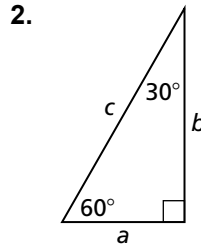
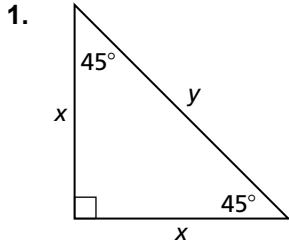
8. The length of a diagonal in a square is 32 inches. Find the perimeter of the square.
9. An isosceles triangle with 30° base angles has an altitude of $\sqrt{3}$ meters. Find the length of the base of the isosceles triangle.

10. Find the area of $\triangle DEF$. Round decimal answers to the nearest tenth.



Practice B

In Exercises 1 and 2, copy and complete the table. Write your answers in simplest form.



x	5		$\sqrt{2}$	
y		$4\sqrt{2}$		24

a	11			
b		9		$5\sqrt{3}$
c			16	

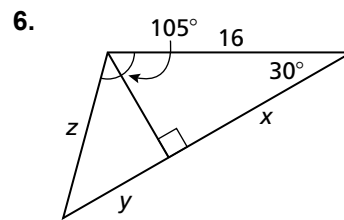
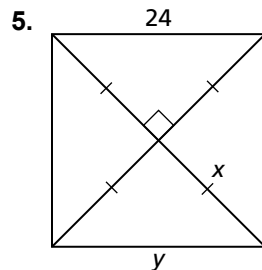
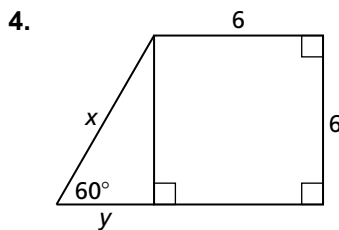
3. The side lengths of a triangle are given. Determine whether each triangle is a 45° - 45° - 90° triangle, a 30° - 60° - 90° triangle, or neither.

a. 5, 10, $5\sqrt{3}$

b. 7, 7, $7\sqrt{3}$

c. 6, 6, $6\sqrt{2}$

In Exercises 4–6, find the values of the variables. Write your answers in simplest form.



7. You build a two-person tent, as shown. How many square feet of material is needed to make the tent, assuming the tent has a floor?

