

4.4**Scatter Plots and Lines of Fit**

For use with Exploration 4.4

Essential Question How can you use a scatter plot and a line of fit to make conclusions about data?

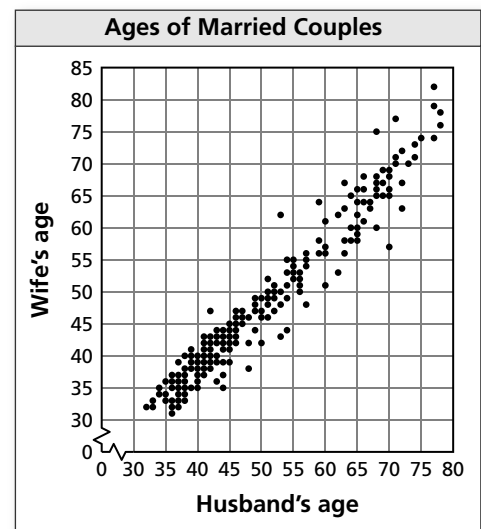
A **scatter plot** is a graph that shows the relationship between two data sets. The two data sets are graphed as ordered pairs in a coordinate plane.

1 EXPLORATION: Finding a Line of Fit

Go to *BigIdeasMath.com* for an interactive tool to investigate this exploration.

Work with a partner. A survey was taken of 179 married couples. Each person was asked his or her age. The scatter plot shows the results.

- a. Draw a line that approximates the data. Write an equation of the line. Explain the method you used.

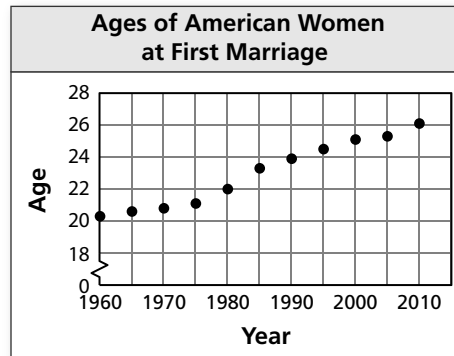


- b. What conclusions can you make from the equation you wrote? Explain your reasoning.

4.4 Scatter Plots and Lines of Fit (continued)**2 EXPLORATION:** Finding a Line of Fit

Go to *BigIdeasMath.com* for an interactive tool to investigate this exploration.

Work with a partner. The scatter plot shows the median ages of American women at their first marriage for selected years from 1960 through 2010.



- Draw a line that approximates the data. Write an equation of the line. Let x represent the number of years since 1960. Explain the method you used.
- What conclusions can you make from the equation you wrote?
- Use your equation to predict the median age of American women at their first marriage in the year 2020.

Communicate Your Answer

- How can you use a scatter plot and a line of fit to make conclusions about data?
- Use the Internet or some other reference to find a scatter plot of real-life data that is different from those given above. Then draw a line that approximates the data and write an equation of the line. Explain the method you used.

4.4

Practice

For use after Lesson 4.4

Core Concepts

Scatter Plot

A **scatter plot** is a graph that shows the relationship between two data sets. The two data sets are graphed as ordered pairs in a coordinate plane. Scatter plots can show trends in the data.

Notes:

Using a Line of Fit to Model Data

- Step 1** Make a scatter plot of the data.
- Step 2** Decide whether the data can be modeled by a line.
- Step 3** Draw a line that appears to fit the data closely. There should be approximately as many points above the line as below it.
- Step 4** Write an equation using two points on the line. The points do not have to represent actual data pairs, but they must lie on the line of fit.

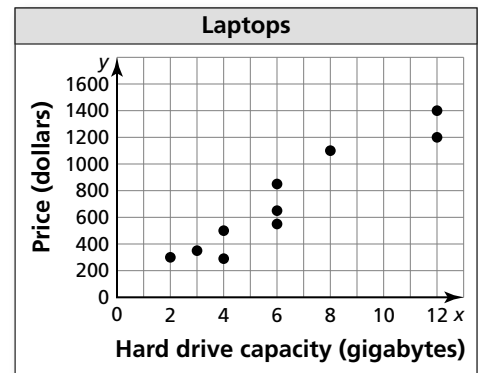
Notes:

Worked-Out Examples

Example #1

INTERPRETING A SCATTER PLOT The scatter plot shows the hard drive capacities (in gigabytes) and the prices (in dollars) of 10 laptops.

- a. What is the price of the laptop with a hard drive capacity of 8 gigabytes?
- b. What is the hard drive capacity of the \$1200 laptop?
- c. What tends to happen to the price as the hard drive capacity increases?
 - a. The laptop with a hard drive capacity of 8 gigabytes costs \$1100.
 - b. The \$1200 laptop has a hard drive capacity of 12 gigabytes.
 - c. The price tends to increase as the hard drive capacity increases.



4.4 Practice (continued)

Example #2

MODELING WITH MATHEMATICS The table shows the total earnings y (in dollars) of a food server who works x hours.

x	0	1	2	3	4	5	6
y	0	18	40	62	77	85	113

- a. Write an equation that models the server’s earnings as a function of the number of hours the server works.
- b. Interpret the slope and y -intercept of the line of fit.

Sample answer:

- a. Use $(0, 0)$ and $(1, 18)$.

The slope of the line is $m = \frac{18 - 0}{1 - 0} = \frac{18}{1}$, or 18.

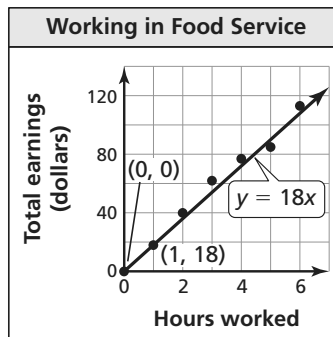
$$y - y_1 = m(x - x_1)$$

$$y - 0 = 18(x - 0)$$

$$y = 18x$$

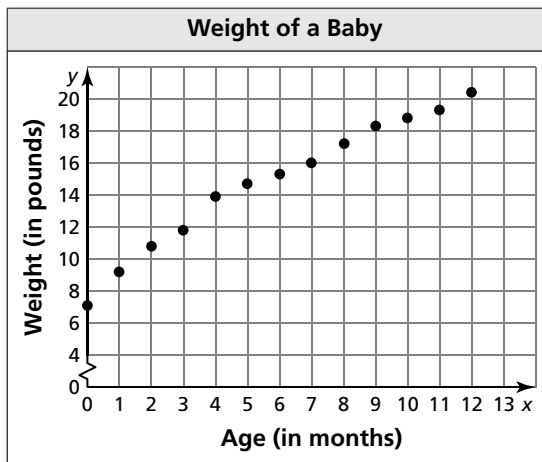
An equation of the line of fit is $y = 18x$.

- b. The slope of the line is 18. This means that the server earns about \$18 per hour. The y -intercept is 0, which means that if the server does not work any hours, then the server will not make any money.



Practice A

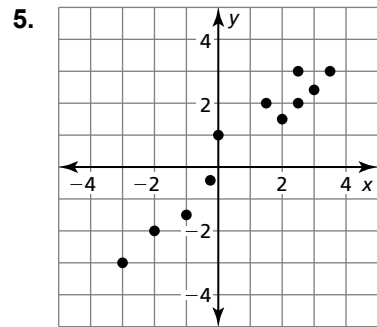
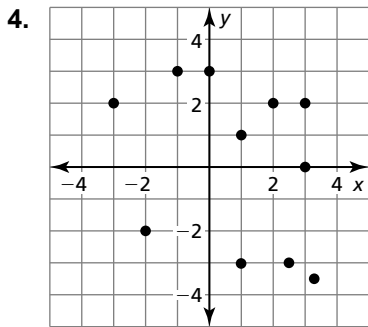
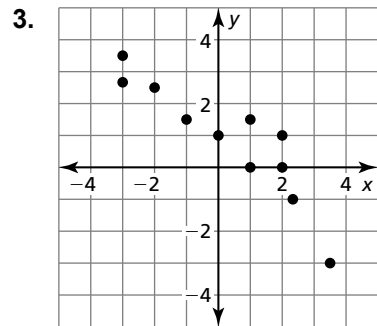
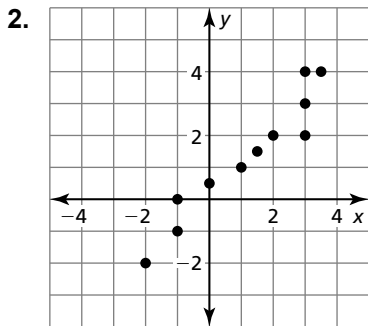
- 1. The scatter plot shows the weights (in pounds) of a baby over time.



4.4 Practice (continued)

- a. What is the weight of the baby when the baby is four months old?
- b. What is the age of the baby when the baby weighs 17.2 pounds?
- c. What tends to happen to weight of the baby as the age increases?

In Exercises 2–5, tell whether x and y show a *positive*, a *negative*, or *no* correlation.



6. The table shows the depth y (in centimeters) of water filling a bathtub after x minutes.

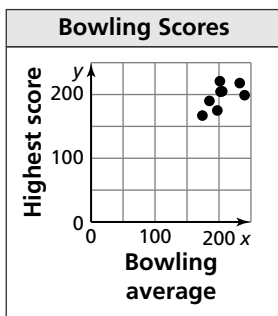
Time (minutes), x	0	2	4	6	8	10	12
Depth (centimeters), y	6	8	11	14	17	20	24

- a. Write an equation that models the depth of the water as a function of time.

- b. Interpret the slope and y -intercept of the line of fit.

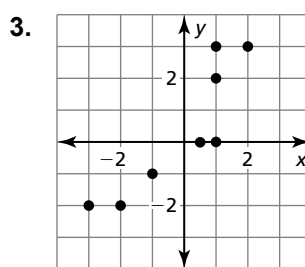
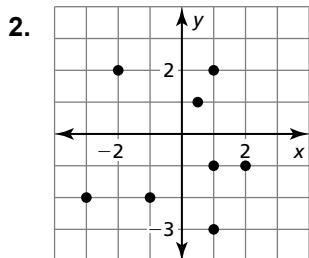
Practice B

1. The scatter plot shows the prior bowling averages of competitors at the bowling tournament and their highest scores during the tournament.



- How many competitors bowled above their average during the tournament?
- Did any bowler(s) bowl their average as their highest score? Explain.
- What are the scores of the competitors with the greatest difference between their bowling average and their highest score?

In Exercises 2 and 3, tell whether x and y show a *positive*, a *negative*, or *no* correlation.



4. The table shows the total number y of rolls of wrapping paper sold by a student after x weeks.

x	1	2	3	4	5	6
y	3	5	9	12	17	24

- Write an equation that models the number of rolls of wrapping paper as a function of the number of weeks.
- Interpret the slope and y -intercept of the line of fit.