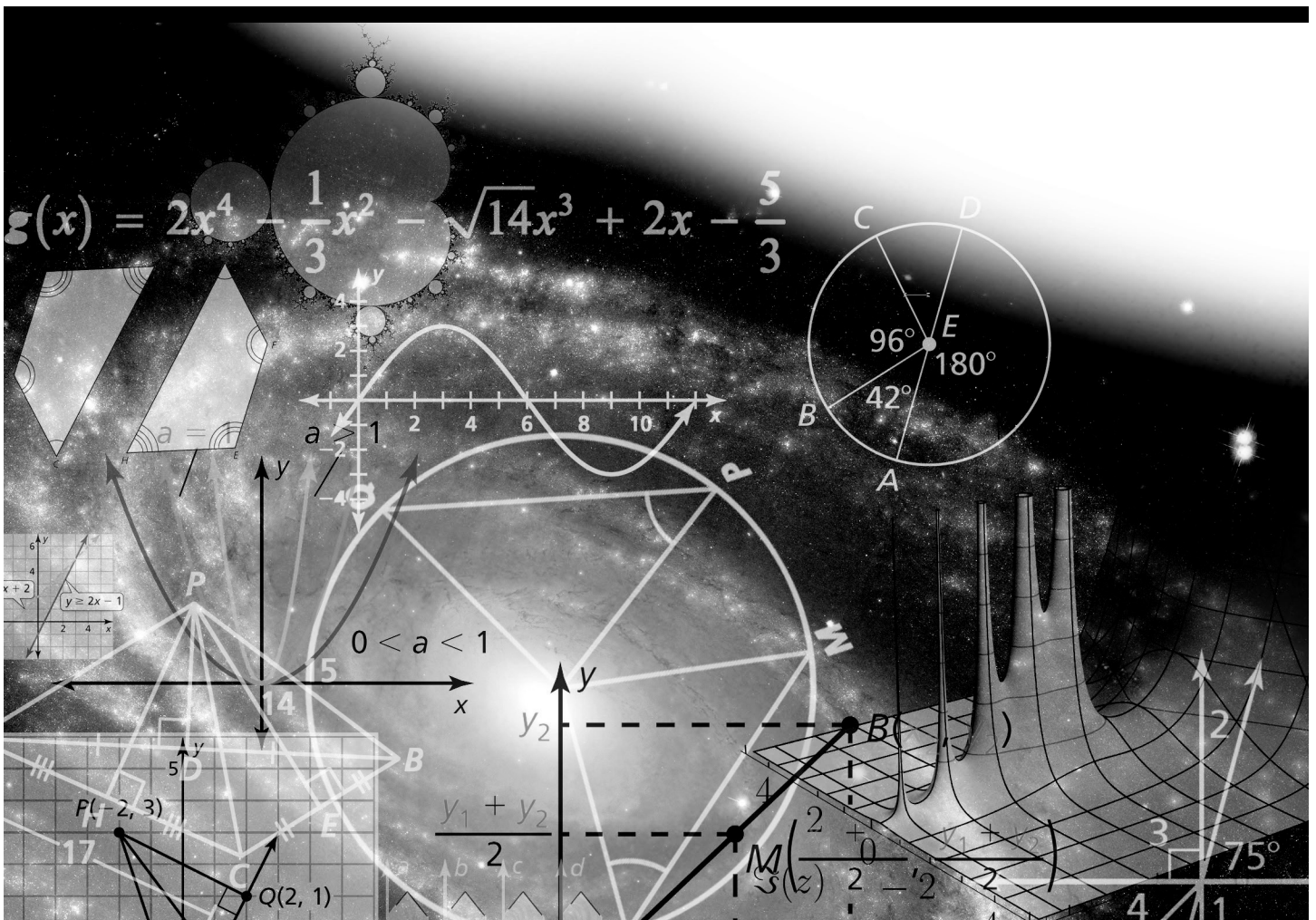


# CHAPTER 3

## Graphing Linear Functions

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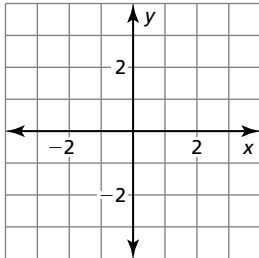


**Chapter  
3**

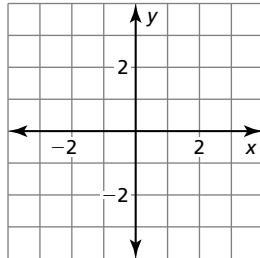
**Maintaining Mathematical Proficiency**

Plot the point in a coordinate plane. Describe the location of the point.

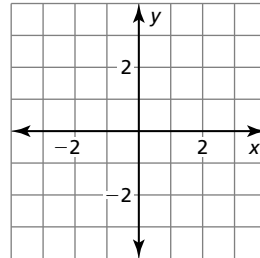
1.  $A(-3, 1)$



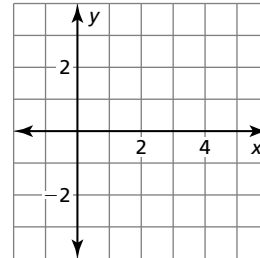
2.  $B(2, 2)$



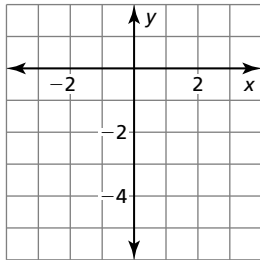
3.  $C(1, 0)$



4.  $D(5, 2)$



5. Plot the point that is on the  $y$ -axis and 5 units down from the origin.



Evaluate the expression for the given value of  $x$ .

6.  $2x + 1; x = 3$

7.  $16 - 4x; x = -4$

8.  $12x + 7; x = -2$

9.  $-9 - 3x; x = 5$

10. The length of a side of a square is represented by  $(24 - 3x)$  feet. What is the length of the side of the square when  $x = 6$ ?

# 3.1

## Functions

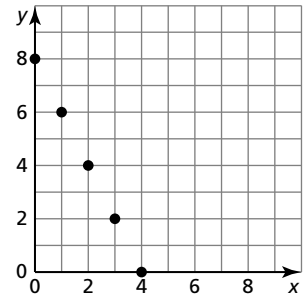
For use with Exploration 3.1

### Essential Question What is a function?

#### 1 EXPLORATION: Describing a Function

Work with a partner. Functions can be described in many ways.

- by an equation
- by an input-output table
- using words
- by a graph
- as a set of ordered pairs



a. Explain why the graph shown represents a function.

b. Describe the function in two other ways.

#### 2 EXPLORATION: Identifying Functions

Work with a partner. Determine whether each relation represents a function. Explain your reasoning.

a.

Input, $x$	0	1	2	3	4
Output, $y$	8	8	8	8	8

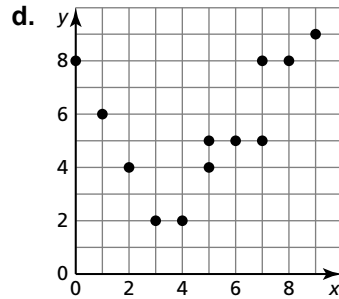
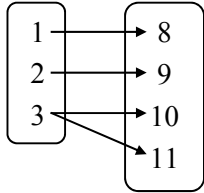
b.

Input, $x$	8	8	8	8	8
Output, $y$	0	1	2	3	4

**3.1 Functions (continued)**

**2 EXPLORATION: Identifying Functions (continued)**

c. Input,  $x$     Output,  $y$



e.  $(-2, 5), (-1, 8), (0, 6), (1, 6), (2, 7)$                       f.  $(-2, 0), (-1, 0), (-1, 1), (0, 1), (1, 2), (2, 2)$

g. Each radio frequency  $x$  in a listening area has exactly one radio station  $y$ .

h. The same television station  $x$  can be found on more than one channel  $y$ .

i.  $x = 2$

j.  $y = 2x + 3$

**Communicate Your Answer**

3. What is a function? Give examples of relations, other than those in Explorations 1 and 2, that (a) are functions and (b) are not functions.

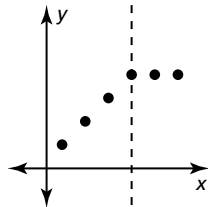
**3.1****Practice**

For use after Lesson 3.1

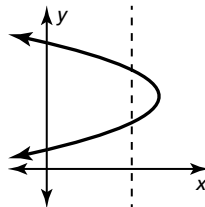
**Notes:****Core Concepts****Vertical Line Test**

**Words** A graph represents a function when no vertical line passes through more than one point on the graph.

**Examples** Function



Not a function

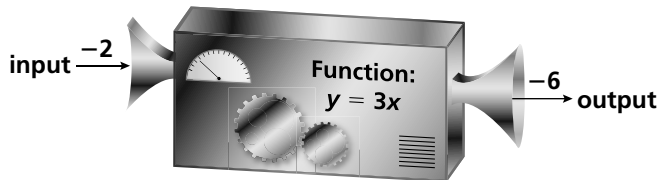
**Notes:**

**3.1 Practice (continued)**

**The Domain and Range of a Function**

The **domain** of a function is the set of all possible input values.

The **range** of a function is the set of all possible output values.



**Notes:**

**Worked-Out Examples**

**Example #1**

**Determine whether the relation is a function. Explain.**

$(7, 4), (5, -1), (3, -8), (1, -5), (3, 6)$

no; The input 3 has two outputs,  $-8$  and  $6$ .

**Example #2**

**MODELING WITH MATHEMATICS** The function  $y = 25x + 500$  represents your monthly rent  $y$  (in dollars) when you pay  $x$  days late.

- a. Identify the independent and dependent variables.
- b. The domain is 0, 1, 2, 3, 4, and 5. What is the range.
  - a. The amount of your monthly rent  $y$  depends on how many days late  $x$  it is when you pay. So,  $y$  is the dependent variable and  $x$  is the independent variable.
  - b. Make an input-output table to find the range.

Input, $x$	$25x + 500$	Output, $y$
0	$25(0) + 500$	500
1	$25(1) + 500$	525
2	$25(2) + 500$	550
3	$25(3) + 500$	575
4	$25(4) + 500$	600
5	$25(5) + 500$	625

The range is 500, 525, 550, 575, 600, and 625.

**3.1 Practice (continued)**

**Practice A**

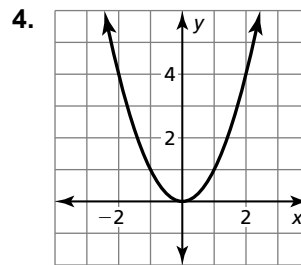
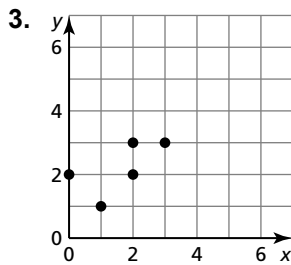
In Exercises 1 and 2, determine whether the relation is a function. Explain.

1.

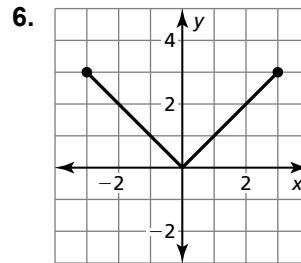
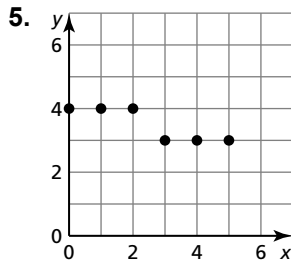
Input, $x$	-2	0	1	-2
Output, $y$	4	5	4	5

2.  $(0, 3), (1, 1), (2, 1), (3, 0)$

In Exercises 3 and 4, determine whether the graph represents a function. Explain.



In Exercises 5 and 6, find the domain and range of the function represented by the graph.



7. The function  $y = 12x$  represents the number  $y$  of pages of text a computer printer can print in  $x$  minutes.

a. Identify the independent and dependent variables.

b. The domain is 1, 2, 3, and 4. What is the range?

## Practice B

In Exercises 1 and 2, determine whether the relation is a function. Explain.

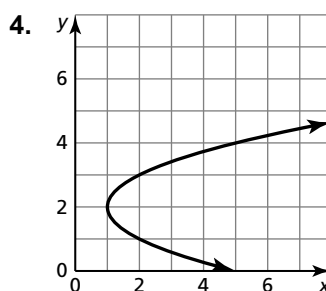
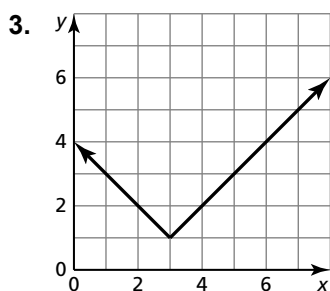
1.

Input, $x$	0	1	3	2	1
Output, $y$	1	5	10	15	20

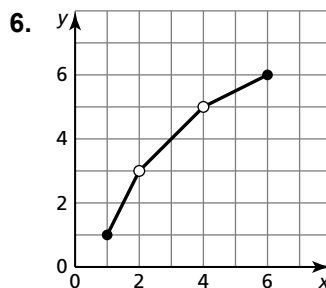
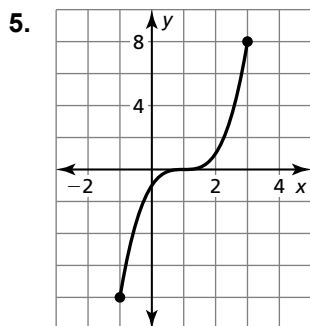
2.

Input, $x$	0	1	2	3	4
Output, $y$	-14	-7	0	7	14

In Exercises 3 and 4, determine whether the graph represents a function. Explain.



In Exercises 5 and 6, find the domain and range of the function represented by the graph.



7. The function  $2x + 1.5y = 18$  represents the number of book raffle tickets  $x$  and food raffle tickets  $y$  you buy at a club event.
- Solve the equation for  $y$ .
  - Make an input-output table to find ordered pairs for the function.
  - Plot the ordered pairs in a coordinate plane.

In Exercises 8–10, find the domain and range of the function.

8.  $y = |x| + 2$

9.  $y = -|x| + 1$

10.  $y = -|x| - 3$